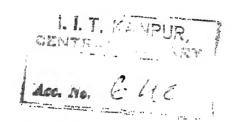
EXPERIMENTAL VERIFICATION OF DYNAMIC SHEAR ANGLE APPROACH FOR THE DETERMINATION OF STABILITY CHART



A Thesis Submitted
In Partial Fulfilment of the Requirements
for the Degree of
MASTER OF TECHNOLOGY



BY
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to the

DEPARTMENT OF MECHANICAL ENGINEERING
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VISHNU BHAGWAN



CERTIFIC ATE

This is to certify that the thesis entitled "Verification of Dynamic Shear Angle Approach for the Determination of Stability Chart" has been carried out under my supervision and this work has not been submitted elsewhere for award of a degree.

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DECEMBER 1, 1971

POST GRADUATE OFFICE
This the fall is been approved
for the count of the Degree of
Masse the mology (All Penn)
in accordance with the
regulations of the last a
Institute of Technology ampur
Dated. 6/12/1/

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SYMOPSIS

The present work is aimed to verify the dynamic shear angle approach for the prediction of stability chart.

A flexible tool holder is designed and fabricated. The flexibility of the tool holder is much higher in the horizontal direction as compared to the vertical direction so that the machine tool workpiece system is assumed to be a single degree of freedom system. Response locus of the tool holder is determined by exciting the tool holder in the horizontal direction and measuring its response in the same direction.

Experimental stability chart is obtained by machining hot finished seamless M.S. tube on L.B.25 Lathe using throw-away-tip-type carbide tools.

A computer program is developed to solve the .
equations of threshold of stability. Theoretical stability
chart is obtained using the computed results.

experimental stability chart shows a close agreement with theoretical results above cutting velocity 70 m.p.m. when the builtup edge is insignificant.

LIST OF NCTATIONS

^A c	Amplitude of Incremental Tangential Cutting Force
í.s	Shear Plane Area
^A t .	Amplitude of Incremental Thrust Force
a ₁	Amplitude of Tool Oscillation
^a 2	Amplitude of wave on Uncut Surface of the workpiece
C	Cutting Coefficient = (D Cos (- 1)/D Sin Ø
D	Stress Ratio = $\frac{1c}{T_s}$
đ	Diameter
$^{ m dF}_{ m c}$	Incremental Tangential Cutting Force
dF_{t}	Incremental Thrust Force
∂ s	Change in Instantaneous Uncut Chip-Thickness
ds ₁	Tool Osciliation
ds ₂	Wave form of Uncut Surface of Work
dd	Change in Rake Argle
Fe	Tangential or Main Cutting Force
F_{ci}	Instantaneous Cutting Porce in Instantaneous
	Cutting Direction
$^{ m F}$ cim	Instantaneous Cutting Force in Mean Cutting Direction
\mathtt{F}_{t}	Thrust Force
$^{ m F}$ ti	Instantaneous Thrust Force Component Mormal to
	Instanlaneous Direction of Cutting
Ttim	Instantaneous Thrust Force Component Normal to
	Mean Direction of Cutting
f	Frequency in Cycles per Second

G	Mean Geometric Lead
Gi	Instantaneous Geometric Lead
K ₁	$Gn_1 + n_2$
L ₁	Length of Chip Before Cutting
L_2	Length of Chip After Cutting
n_1	Shear Angle-Chip Thickness Coefficient = 30/3s
n ₂	Shear Angle-Rake Angle Coefficient = $\partial \emptyset / \partial A$
r	Mean Radius of Workpiece
R	Resultant Force
s	Mean Uncut Chip-Thickness
s _i	Instantaneous Uncut Chip Thickness
s ₁	Uncut Chip Thickness (Feed Rate)
s_2	Cut Chip Thickness
T	Time Period Per Revolution, Vibration Period
${ t T}_{f c}$	Cutting Stress
Ts	Shearing Stress
t	Time
v, V	Mean Cutting Speed
X	Distance Measured in the Mormal Direction to
	Machined Surface
, L	Mean Rake Angle
$\lambda_{\mathtt{1}}$	Instantaneous Rake Angle
β 13 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Angle of Friction at Rake Face of Tool
/3 1	Angle Between Mean and Instantaneous Direction of
	Cutting

Υ	Mean Angular lead of Free End of Shear Plane
Y i	Instantaneous Ingular Lead of Free End of Shear
	Plane
θ	Phasing Between Uncut Surface Vaveform and Tool
	Oscillation
λ	Wave Length
μ .	Overlap Factor .
Ø	Mean Shear Angle
$arphi_{ exttt{i}}$	Instantaneous Shear Angle Referred to Instantaneous
	Cutting Direction
Ψc	Phase of Incremental Tangential Cutting Force
ψt	Phase of Incremental Thrust Force
/ · ·	ingular Speed in Cadians Per Second.

CHIPTER 1

INTRODUCTION

Metal cutting process is often associated with vibrations between tool and work piece. These vibrations cause poor surface finish, reduce tool-life, affect machining accuracy and reduce production rate.

Three types of vibrations occur in machine tools:

- (a) Forced vibrations are caused by the unbalancing effects in the machine tool work piece system.
- (b) Free vibrations are caused due to the shock transmitted through the foundation from the neighbouring machines.
- (c) Self excited vibrations are also called chatter vibrations. Chatter is caused by interaction of cutting process with the dynamic behaviour of the machine tool structure.

Forced and free vibrations are well understood and can be eliminated easily. Chatter vibrations pose a greater problem. These vibrations are due to the dynamic instability of the machine tool system.

In order to predict the dynamic stability region of machine tool system, one has to analyse:

- (a) Dynamics of machine Tool Structure, and
- (b) Dynamics of Cutting process.

1.1 Dynamics of Lachine Tool Structure

Dynamic behaviour of a structure is represented by harmonic response locus of the structure. The response of the machine tool structure in the direction of applied harmonic exciting force is called the direct response of the structure. Direct response per unit force is termed direct receptance.

The response of the structure in the direction perpendicular to the applied harmonic exciting force is termed the cross response of the structure. Cross response per unit force is called the cross receptance.

The receptance of a structure can be represented by a complex number, (a+ib). (Ref. 1,2). Where a represents the inphase component of receptance and b represents the out of phase component of the receptance. If (a+ib) is plotted in such a way that 'a' is plotted as abcissa and 'b' as ordinate, then the harmonic receptance locus is obtained.

1.2 Dynamics of Cutting Process

During chatter vibration, the tool vibrates relative to the work piece and cutting parameters such as depth of cut, rake angle and cutting speed etc., undergo

cyclic vibration which lead to non-steady-state metal cutting.

Thusty and Polacek (Ref.2) assumed that variation in cutting forces depends only upon the chip thickness variation caused by relative vibration of tool and workpiece.

Tobias and Fishnick (Ref.4) assumed that variation in cutting forces under dynamic cutting conditions depends upon chip thickness variation, cutting speed variation and tool penetration rate.

Das (Pef.5,6) used the concept of universal machinability index for predicting the dynamic cutting forces. He also considered that shear plane does not vary under dynamic cutting conditions.

Knight (Ref.7) used the results of Das and Tobias (Ref.6) for the prediction of the stability of a simplified machine tool system.

The previous research workers have tried to predict the dynamic cutting forces from the characteristics of steady state cutting forces. However the theoretical analysis has not shown satisfactory agreement with experimental results.

Kainth (Ref.8) gave a theoretical model for predicting dynamic forces from the results of the steady state cutting tests. He considered the shear plane length as the most influential parameter in the steady state metal cutting. Considering dynamic shear angle, he gave a model (Fig.1) of dynamic cutting forces from which the expressions for incremental tangential cutting force dF_c and incremental thrust force dF_t can be written as follows:

$$dF_c = A_c \sin \left(\approx t + \varphi_c \right) \tag{1.1}$$

$$dF_{t} = L_{t} \sin (\omega t + \varphi_{t})$$
 (1.2)

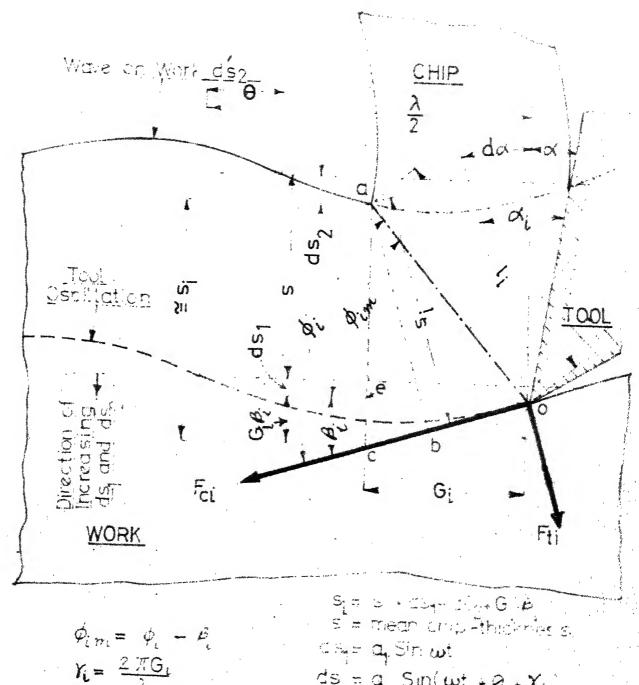
where,

 ^{-1}c = implitude of the incremental cutting force $^{-1}dF_{c}$

$$= \begin{bmatrix} \{i_{c1} \cos \varphi_{c1} - i_{c2} \cos(\theta + \varphi_{c2})\}^{2} \\ + \{i_{c1} \sin \varphi_{c1} - i_{c2} \sin(\theta + \varphi_{c2})\}^{2} \end{bmatrix}$$
 (1.3)

 \mathcal{C} = Phase angle of the Incremental cutting force.

= arctan
$$\left[\frac{A_{c1} \sin \frac{\pi}{f}}{A_{c1} \cos \frac{\pi}{f}} - \frac{A_{c2} \sin \left(\theta + \frac{\psi}{c2}\right)}{A_{c2} \cos \left(\theta + \frac{\psi}{c2}\right)}\right] (1.4)$$



 $Y_i = \frac{2\pi G_i}{\lambda}$

ds = a Sin(wt +0 + Yi)

GEOMETRY OF DYNAMIC CUTTING

(WAVE -ON - WAVE CUTTING)

 $\psi_{\rm t}$ = Phase angle of the incremental thrust force

=
$$\arctan \frac{i_{t_1} \sin \psi_{t_1} - i_{t_2} \sin (\theta + \psi_{t_2})}{-i_{t_1} \cos t_1 - i_{t_2} \cos (\theta + \psi_{t_2})}$$
 (1.6)

Phase angles $\psi_{\rm c}$ and $\psi_{\rm t}$ are relative to the oscillation of the tool.

$$\frac{1}{4} = \frac{T_{c} W_{1}}{\sin \emptyset} / (1 - n_{1} s \cot \emptyset)^{2} \div \left\{ (1 - K_{1}) \cot \emptyset - c \right\}^{2} \\
(2 \pi s/\lambda)^{2} (1.7)$$

$$\psi_{c1} = \arctan \left[\frac{\left\{ (1 - K_{1}) \cot \emptyset - c \right\} \left\{ (2 \pi s/\lambda) \right\}}{1 - n_{1} s \cot \emptyset} \right] (1.8)$$

$$\Delta_{t1} = \frac{T_{c} W_{1}^{2}}{\sin \emptyset} / \left\{ (1 + c \cot \emptyset) - K_{1}(1 + 2c \cot \emptyset) \right\}^{2} + \left\{ (1 + c \cot \emptyset) - K_{1}(1 + 2c \cot \emptyset) \right\}^{2}$$

$$\psi_{t1} = \arctan \left[\frac{\left\{ (1 + c \cot \emptyset) - K_{1}(1 + 2c \cot \emptyset) \right\} 2 \pi s/\lambda}{c - n_{1} s (1 + 2c \cot \emptyset)} \right] (1.9)$$

$$n_{c2} = \frac{T_c}{\sin \theta} \frac{I_{a2}}{\theta} (1 - n_1 \operatorname{s Cot} \theta)$$
 (1.11)

$$\psi_{c2} = \frac{2\pi}{2\pi} \cdot 2\pi s \cot \mathcal{E} / \lambda$$
 (1.12)

$$L_{t2} = \frac{T_c \sqrt{a_2}}{\sin \emptyset} \left\{ c - L_1 s (1 + 2c \cot \emptyset) \right\}$$
 (1.13)

$$\psi_{t2} = Y = 2\pi$$
 $2\pi s \cot \emptyset/\lambda$ (1.14)

Kainth carried out experiments to measure dynamic cutting forces and showed good correlation between experimental and theoretical results.

1.3 Determination of Threshold of Stability

where,

Under the presence of chatter vibration, cutting forces (F_c + dF_c) and (F_t + dF_t) act on the system as shown in Fig. 2.

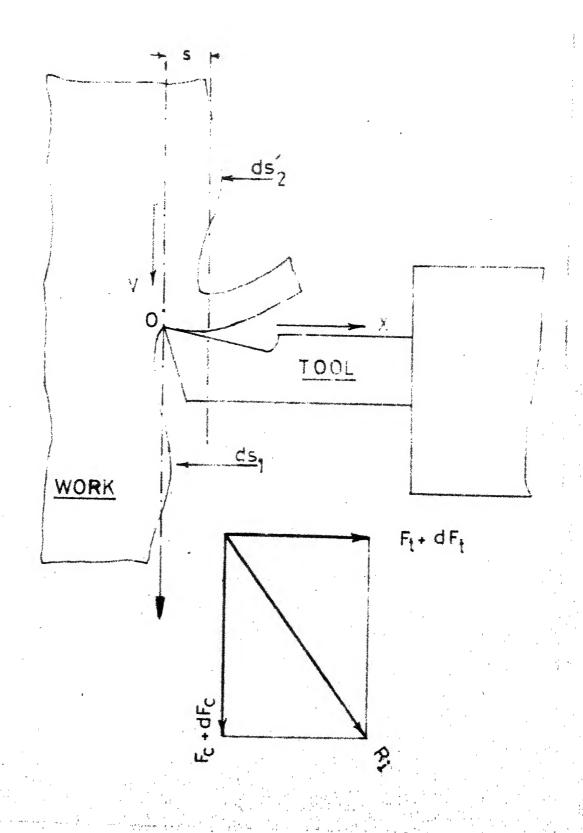
Knight (Ref.7) gave the following expression for the displacement of tool in x-direction :

$$X(t) = -(g + ih) dF_t - (p + iq) dF_c$$
 (1.15)

(g + ih) = direct receptance of structure

(p + iq) = cross receptance of structure

It the threshold of stability, vibration magnitude will remain constant irrespective of time.



NOMENCLATURE OF CUTTING PROCESS

<u>FIG.2</u>

Hence vibration can be written in the form,

$$X(\tau) = h_0 e^{i\omega t}$$

$$= ds_1$$
(1.16)

= tool vibration

$$ds_2^t = A_0 e^{i\omega(t-T)}$$
 (1.17)

= wave generated on the work piece

$$ds_2 = A_0 e^{i \omega(t-T) + \gamma}$$
(1.13)

= value of ds_2 ' at a mean angular lead of Υ ahead of tool point '0'

Kainth (Ref.8) used his analysis to solve equation (1.15) and gave the following conditions for the threshold of stability:

$$1 = -\frac{T_{c} W}{\sin \varphi} (g + ih) \begin{cases} \{c - n_{1} s (1 + 2c \cot \varphi)\} \\ (1 - \mu \cos \varphi + i \mu \sin \varphi) \end{cases}$$

$$+ \frac{i \omega s}{V} \{(1 + c \cot \varphi)\}$$

$$- \frac{T_{c} W}{\sin \varphi} (p + iq) \begin{cases} (1 - n_{1} s \cot \varphi) (1 - \mu \cos \varphi) \\ + i \mu \sin \varphi + \frac{i \omega s}{V} \end{cases}$$

$$\{(1 - K_{1}) \cot \varphi - c\} \qquad (1 (1.19)$$

In equation (1-19) med and imaginary parts can be put to zero separately,

(1-21)

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CHAPTER 2

EXPERIMENTAL INVESTIGATION OF THE STABILITY CHART

2.1 Introduction

Present work is aimed to verify the dynamic shear angle approach for the prediction of stability of machine tools from the results of steady state cutting tests. For analytical simplicity a flexible tool holder is designed such that it is essentially a single degree of freedom system. Direct harmonic response locus of the tool holder is obtained by exciting the tool holder by an electromagnetic shaker. Stability chart is determined by carrying out cutting tests on H.M.T. L.B.-25 Lathe.

2.2 Flexible Tool Holder

A flexible tool holder is designed and fabricated as shown in Fig. 3. Tool is secured in a block which is mounted on four leaf springs. Each leaf spring is screwed with the base of the tool holder at two points. This ensures rigid fixing of the leaf springs with the base of the tool holder. Other ends of the leaf springs are screwed with the block carrying the tool.

Head of the tool holder is joined to the block with the help of four bolts. By changing the mass of the head, supported on the leaf springs the natural frequency of the tool holder can be changed.

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Leaf springs are designed in a manner such that the section modulus of these springs in y-direction is sixteen times the section modulus in x-direction. This is done to ensure that the tool holder is essentially a single degree of freedom system.

2.2.1 Response Locus of the Tool Holder

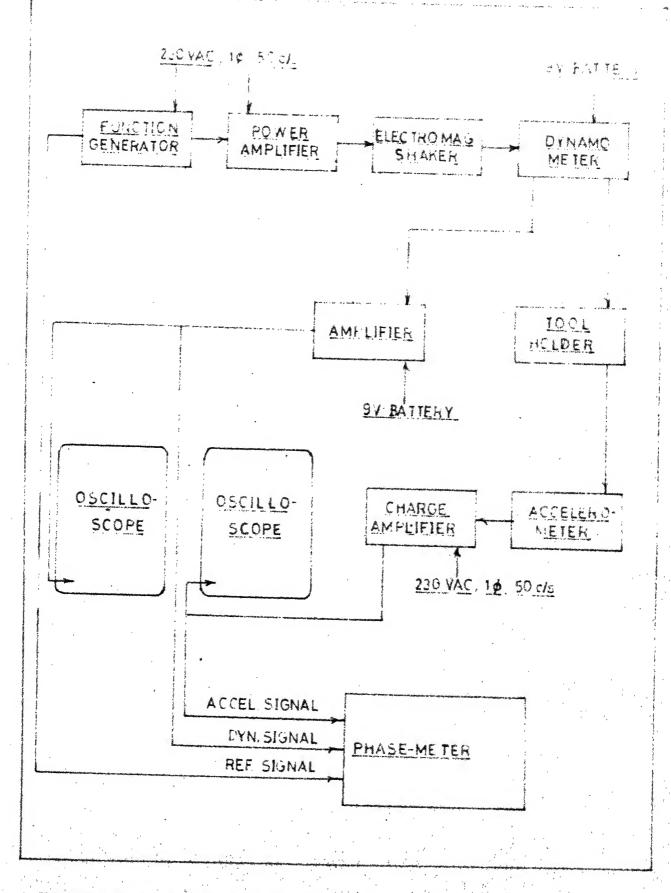
Harmonic response locus of the tool holder is required for solving the equations of threshold of stability. This is determined by exciting the tool holder in x-direction and measuring the output of the tool holder in the same direction.

The block diagram of the instrumentation used is shown in Fig. 4. Photograph of the set up is shown in Fig. 5.

The electromagnetic shaker is placed in horizontal direction and is clamped to the base plate by a metal strip. To measure the force amplitude a dynamometer* is connected with the shaker through a right hand and left hand bolt. Lock nuts are provided to ensure the rigid fixing of dynamometer with the shaker. A mild steel bar threaded at both ends is used to connect the dynamometer with the tool holder. Tool holder is rigidly fixed with base plate through four bolts.

Sinusoidal input to the shaker is provided by a function generator through a power amplifier.

^{*} Dynamometer designed by Loomba (Ref.9) was used.



BLOCK DIAGRAM of THE INSTRUMENTATION USED for RESPONSE LOCUS of THE TOOL HODER

FIG.4

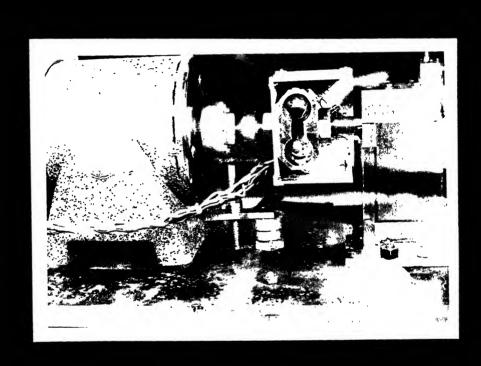


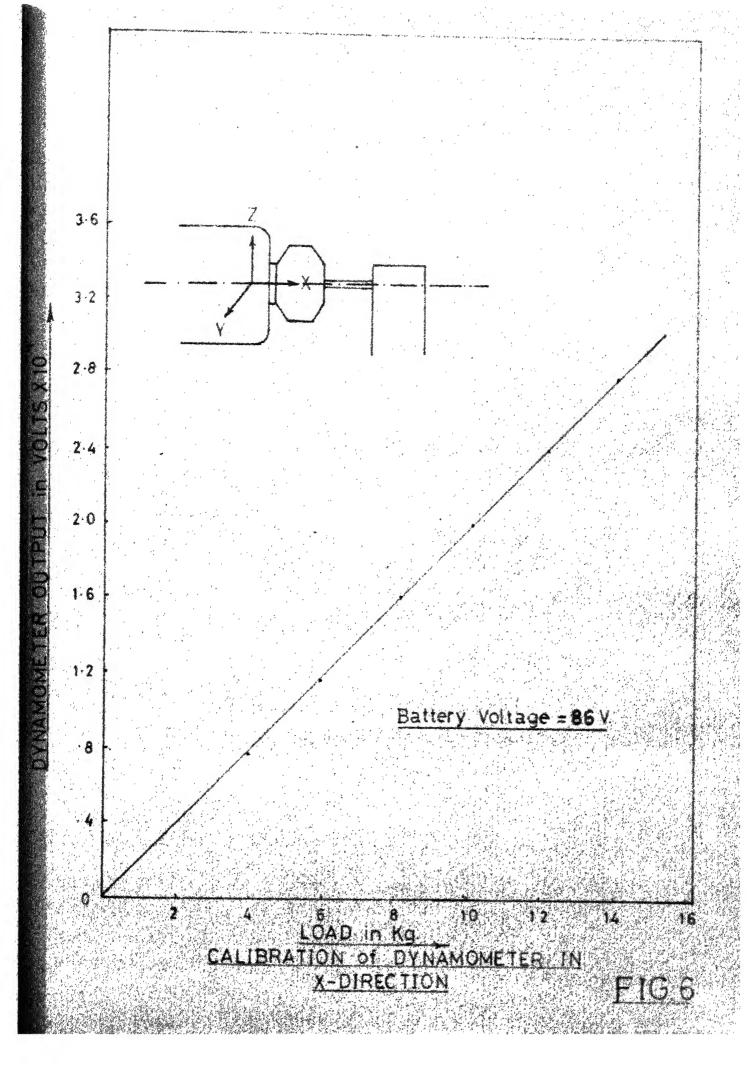
FIG. 5 - SET UP FOR RESPONSE LOCUS OF THE TOOL-HOLDER

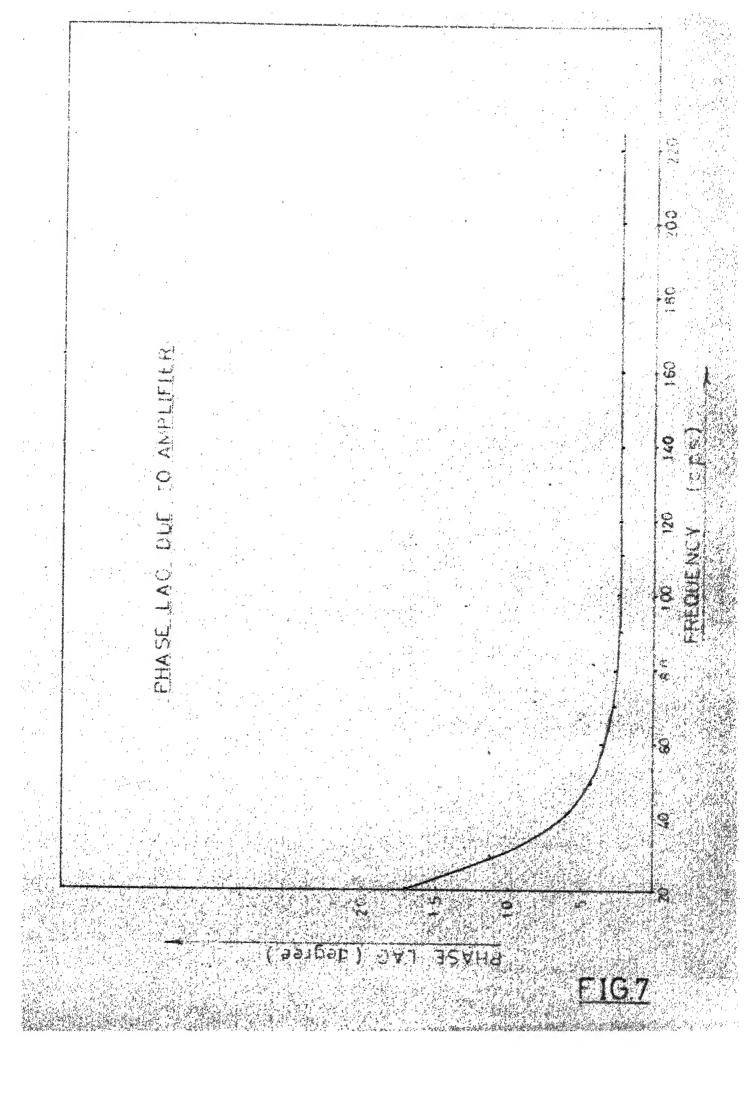
A tri-axial accelerometer is fixed on the top of the tool holder to measure vibrations of the tool holder in all the three directions. Output of the accelerometer is amplified in a charge amplifier and displayed on an oscilloscope.

Dynamometer is calibrated statically by using standard weights. Calibration curve of the dynamometer is shown in Fig. 6. Cross response of the dynamometer in z direction was found to be negligible.

Phase difference between the input and the output signals can be determined by a phase-meter provided both the signals are of required magnitude. The reference signal should be above 22 V, pk-pk. and the other signal termed as input signal should be above 16 mV, pk-pk. In the present case dynamometer signal is of the order of a fraction of millivolts and accelerometer signal is of the order of a few hundred millivolts. Dynamometer signal is amplified by an amplifier having amplification factor of 400. The phase characteristic of the amplifier is determined separately and is shown in Fig. 7.

Phase difference between the dynamometer signal and the accelerometer signal is computed after measuring the phase difference of the two signals separately with respect to a reference signal. Reference signal is taken from the function generator.





. 19

2.2.2 Procedura

All the instruments are switched on, for 10 to 15 minutes, for stabilising the instruments before conducting experiment.

Force level of the shaker is kept constant at 7.5 kg.pk. which corresponds to 3 mV pk-pk output signal of the dynamo-meter. The signal is displayed on the oscilloscope and its amplitude is adjusted by varying the input to the shaker.

For a particular frequency, the force level is first adjusted. Output of the accelerometer in the direction of excitation is read from the oscilloscope. Inphase and quadrature components of the dynamometer signal and of the accelerometer signal with respect to the reference signal are measured soperately by the phasemeter. The procedure is repeated by seeping the frequency in steps of 2.5 cps.

Phase difference between the dynamometer signal and accelerometer signal is computed by substracting the measured phase differences of one signal from the other signal. Displacement signal leads the acceleration signal by 180°. An account of it is made while computing the phase difference. Phase shift in the dynamometer amplifier is also taken into account.

As the exciting signal is harmonic, displacement is determined by dividing the amplitude of the accelerometer signal by ω^2 , where ω is the exciting frequency.

The output of the accelerometer in the two directions other than the direction of excitation is below 5 percent of the output in the direction of excitation. Hence the tool holder can be considered, essentially, a single degree of freedom system.

Inphase component of the accelerometer output is plotted as abcissa and the out of phase component of the accelerometer signal is plotted as ordinate. The frequency of oscillation is indicated along the curve. The curve thus obtained is called the harmonic response locus of the tool holder and is shown in Fig. 8.

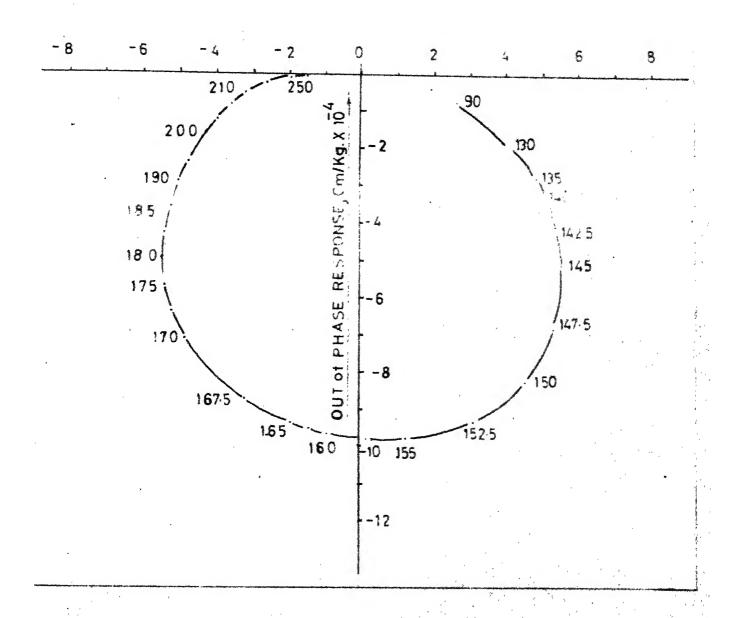
2.3 Experimental Stability Chart

For determining stability chart experimentally, H.M.T. L.E.-25 Lathe being very sturdy is selected. As the tool-holder is much more flexible in x-direction as compared to y-direction, hence the machine tool work piece system can be assumed to be a single degree of freedom system.

The photographs of the emperimental set up are shown in Fig. 9 and Fig. 10.

For determining stability regions closer steps of speed, as compared to the steps available with L.B.-25, are desired. For obtaining closer steps of speeds, motor of the lathe is replaced by a continuous variable speed D.C.Motor.

IN PHASE RESPONSE; Cm/kg x 104



RESPONSE LOCUS of THE FLEXIBLE TOOL HOLDER

F1G.8

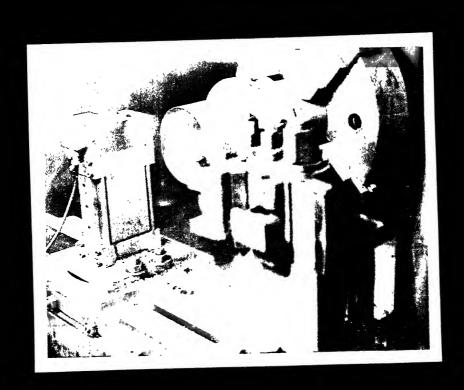
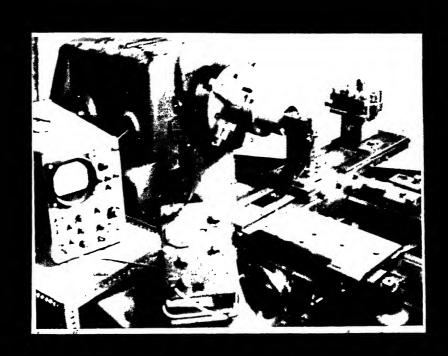


FIG. 9 - SET UP FOR EXPERIMENTAL STABILITY CHART



PIG.10 - INSTRUMENTATION FOR EXPERIMENTAL STABILITY CHART

A special mounting is designed and fabricated for this purpose.

Hot finished seamless M.S. tube having .25% carbon was used for experiment. Carbide throw-away-tool-tips with 5° rake angle were used for machining tube specimens of 8" length at a feed of .05 mm per revolution. Higher feeds could not be used due to the lower capacity of the variable speed motor as compared to the standard motor supplied with the lathe.

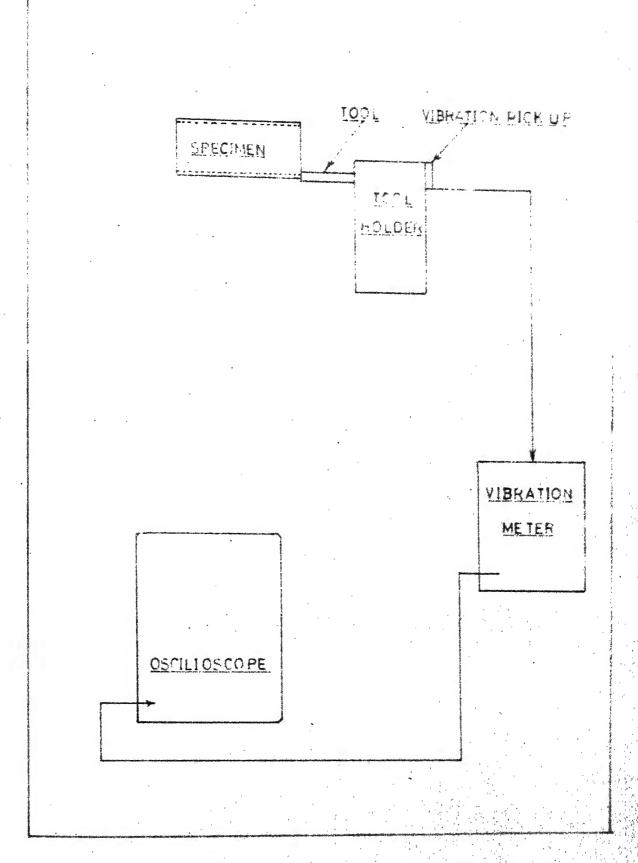
2.3.1 Instrumentation

Block diagram of the instrumentation used is shown in Fig. 11. A vibration pick up is attached at the back of the tool holder. The pick up is suitable for a frequency range of 2-20000 cps. The pick up is connected to the vibration-meter for measuring the magnitude of the vibration. Output of the vibration meter is displayed on the storage oscilloscope for measuring its frequency.

A techometer is used to measure the speed of the driving motor. Spindle speed of the lathe is computed by knowing the gear ratio and the speed of the original motor.

2.3.2 Procedure

Tube specimens of 8" length are turned with a mean radius of 54 mm. Work piece is mounted in the adopter which is used to avoid the centering of individual pieces.



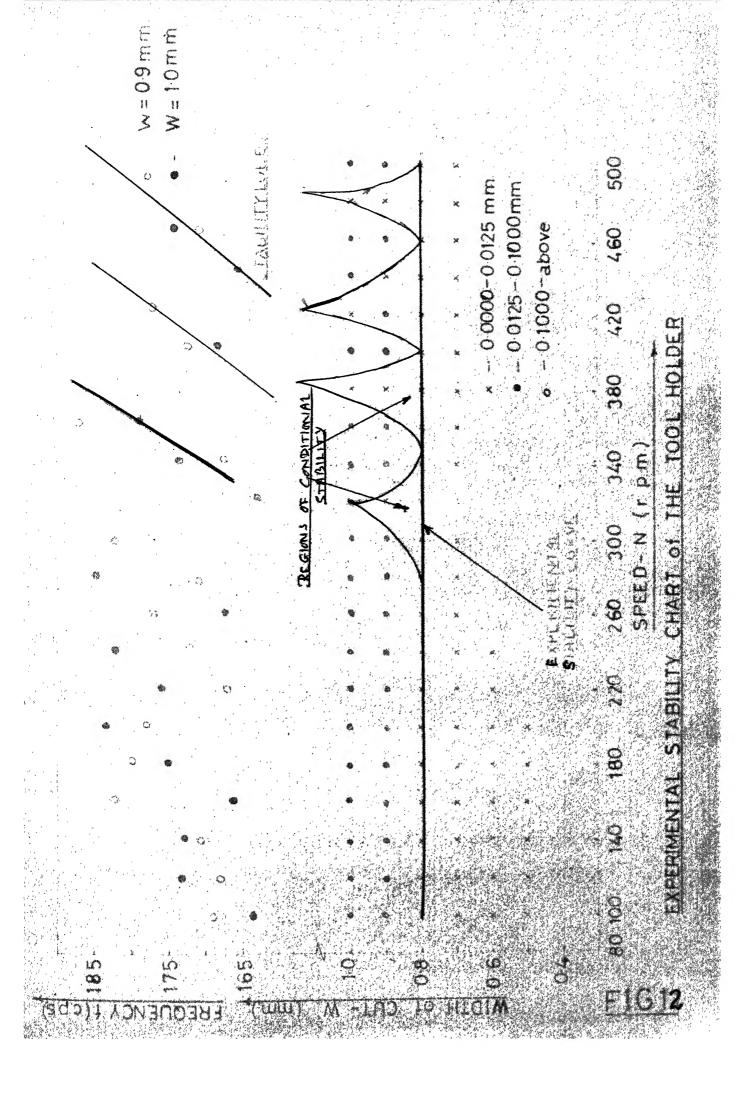
BLOCK DIAGRAM of SEI UP FOR EXPERIMENTAL
STABILITY CHARI

E1G.11

Thickness of the tube is varied from .5 mm to 1 mm in steps of .1 mm after each set of tests for a range of cutting speeds at a particular thickness.

Amplitude of vibration is measured by the help of the vibration meter and the frequency of vibration is obtained by displaying the signal on the storage oscilloscope. Fresh cutting edge is used for each test. After every reading the wavy surface left on the workpiece, by the previous test, is removed by the help of back tool post. Three readings are taken for each speed for a particular width of cut. Tests are conducted for spindle speeds of 100 to 500 rp.m. in steps of 20 rp.m.

Figure 12 shows plots of frequency versus revolutionary speed. Width of cut is also plotted against speed. The upper portion of the graph shows straight lines corresponding to stability lobes. Stability lobes are drawn touching the points showing stability Such that all the points showing vibrations lie above the boundaries of the lobes. An envelope to those stability lobes is termed as threshold of stability curve.



CHAPTER 3

THEORETICAL STABILITY CHART

3.1 Introduction

In the present study; machine tool system is assumed a simplified single degree of freedom system. Hence the cross receptance (p+iq) is taken zero. Also in orthogonal cutting value of overlap-factor to is one. Hence for the present case equations of the threshold of stability reduce to the following equation.

$$\frac{1}{V} = -\frac{T_{c}}{\sin \varphi} \begin{bmatrix} \left\{g(1-\cos \varphi')-h \sin \varphi'\right\} \left\{c-n_{1}s(1+2c \cot \varphi)\right\} \\ -\frac{h\omega s}{V} \left\{(1+c \cot \varphi)-K_{1}(1+2c \cot \varphi)\right\} \end{bmatrix}$$

$$0 = \begin{bmatrix} \left\{h \left(1-\cos \varphi'\right)+g \sin \varphi'\right\} \left\{c-n_{1}s \left(1+2c \cot \varphi\right)\right\} \\ +\frac{g\omega s}{V} \left\{(1+c \cot \varphi)-K_{1}(1+2c \cot \varphi)\right\} \end{bmatrix}$$

$$(3.1)$$

where,
$$\Theta' = \frac{\omega}{n} \left(1 - \frac{s \cot \emptyset}{2 \pi r n}\right) \tag{3.3}$$

Theoretical stability chart can be predicted by solving the equations (3.1) and (3.2). For this purpose, response locus of the tool-holder and the variation of the following cutting parameters with cutting speed is required:

- (a) Cutting stress 'Tc'
- (b) Shear angle 'ø'
- (c) Stress ratio 'D' and
- (d) Shear angle coefficients n_1 and n_2 .

Variation of ${}^{\text{T}}c^{\text{T}}$, ${}^{\text{T}}D^{\text{T}}$, ${}^{\text{T}}n_{1}^{\text{T}}$ and ${}^{\text{T}}n_{2}^{\text{T}}$ with cutting speed

Kainth (Ref.8) has given graphs for the variation of 'Tc', 'D', 'n' and 'n' with cutting speed. He also used hot finished M.S. tube with .25% carbon and carbide tool with 5° rake angle. Cutting stress 'Tc', 'D' and 'n' are independent of chip thickness (Ref.8) and their variation with cutting speed is shown in Fig. 13 and 14. The variation of n with cutting speed for chip thickness of .05 mm is obtained by intrapolating the results of Kainth (Ref.8). The intropolated curve is shown in Fig. 14.

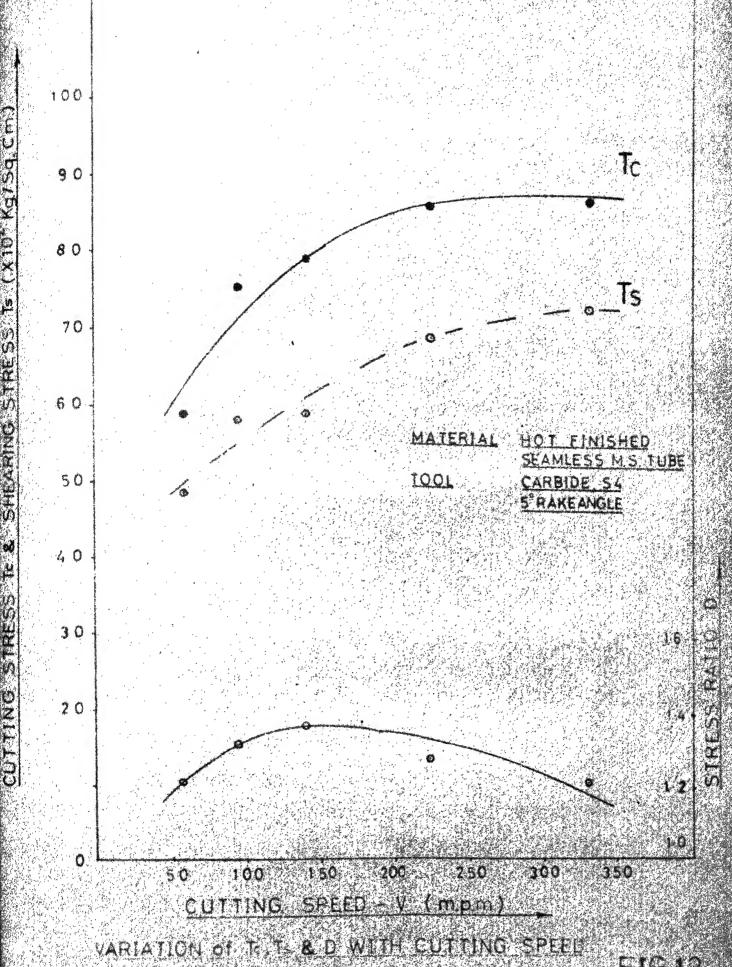
By using the multiple regression analysis, the following polynomiaks are fitted to the curves given in Figs. 13 and 14.

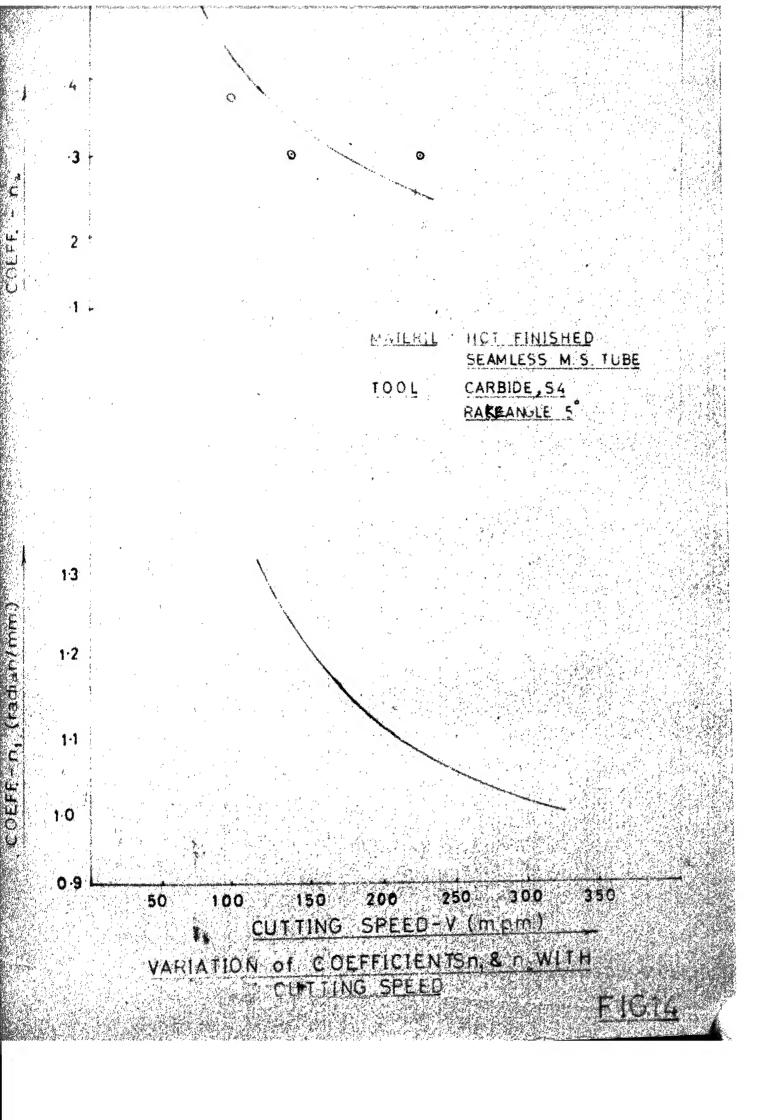
$$T_c = 2.48 + 15.14 (V/10) - 1.1 (V/10)^2 + .04(V/10)^3$$

$$- .00043 (V/10)^4$$

$$D = .768 + 1.14 (V/10) - .78 (V/100)^2 + .215 (V/100)^3$$

$$- .02 (V/100)^4$$





$$n_1 = 1.348 (V/100)^{-.2715}$$

$$n_2 = 3.4 \text{ (VX 3.281)}^{-.38}$$

where $T_c = Cutting stress in kg/mm^2$

D = Stress Ratio

n₁ = shear angle-chip thickness coefficient radians/mm.

n₂ = shear angle-rake angle coefficient

V = cutting velocity in m.p.m.

3.3 Variation of Shear Angle \emptyset with Cutting Speed V

Experiments are carried out for determining the variation of shear angle with cutting speed.

Mild steel specimen is machined to give a mean radius of 54 mm and width of cut of 2.2 mm. Carbide tool with 5° rake angle is used for cutting. Feed of .05 mm/rev is kept constant.

Method of length measurement is used to determine shear angle. A 'Vee' groove is cut on the tube, longitudinally. Chips collected during cutting carry nothes corresponding to the groove. Chips equivalent of 4 to 5 revolutions are collected and measured, thus giving the length of chip after machining. The notches on the chips collected are used to determine the number of revolutions of the work-piece during cutting.

Therefore initial uncut chip length L_1 is,

where r = Mean radius of work piece

N = Number of revolutions for which chip length is measureâ

If L_2 is the chip length measured, then the chip thickness ratio ${}^t\mathbf{r}_c{}^t$ is

$$r_c = \frac{s_1}{s_2} = \frac{L_2}{L_1}$$

and shear angle Ø is,

$$\emptyset = Arctan \left(\frac{r_c \cos \alpha}{1 - r_c \sin \alpha} \right)$$

where Z is the rake angle of the tool.

The variation of shear angle \emptyset with cutting speed is shown in Fig. 15.

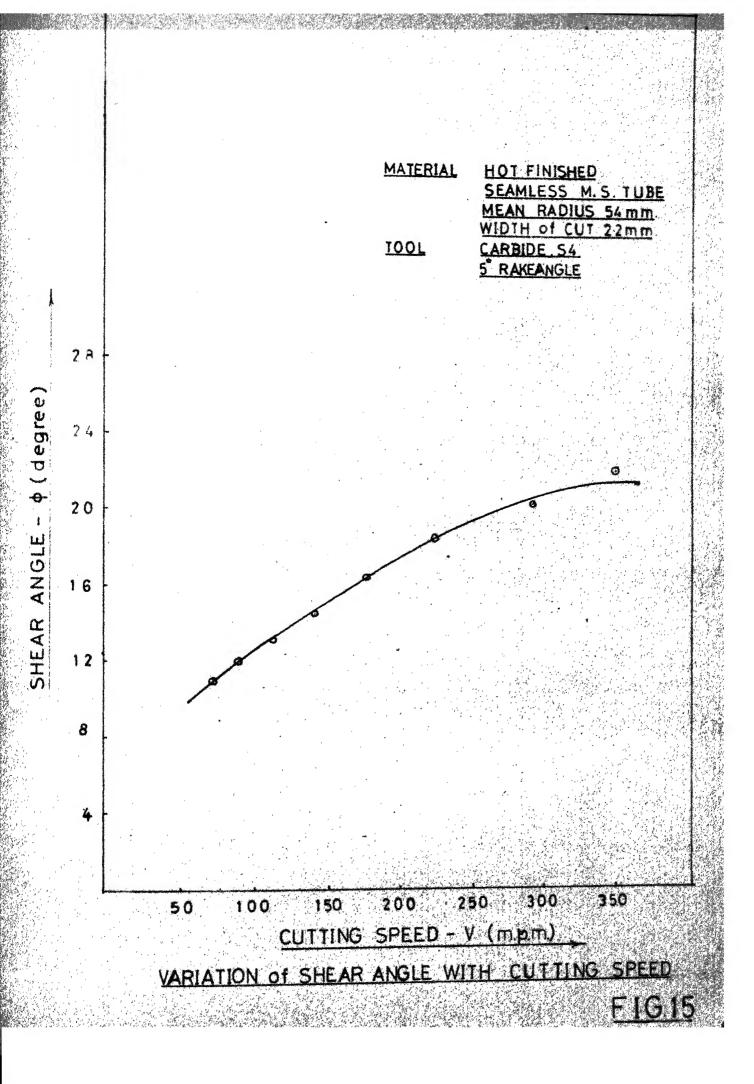
The following second order polynomial is fitted to the above curve,

 $\emptyset = 6.482 + .6813(V/10) - .0067 (V/10)^2$

where Ø is in degrees and V is in m.p.m.

3.4 Solution of the Equations of Threshold of Stability

For a particular frequency, roots of equation (3.2) are determined and for these roots values of widths of cut are calculated from equation (3.1).



A computer program is developed to solve equations (3.1) and (3.2). The program is given in Appendix.

So treh for the roots of the equation 3.2 starts from 60 r.p.m. for a particular frequency. Frequency range of 160 c.p.s. to 230 c.p.s. is used in steps of 2.5 c.p.s. At these frequencies values of inphase and out of phase components a and b respectively is determined from the harmonic response locus of the tool-holder.

For a particular frequency function value of equation 3.2 is calculated, at steps of 0.3 r.p.m. At each of the steps values of cutting parameters \emptyset , D, n_1 and n_2 are taken from the fitted curves. Whenever, at two consecutive steps, the function value changes its sign, a root is expected in the step. Steefanson's search technique is used to determine the root where the function value approaches 10^{-5} . All the roots are searched for a frequency and the whole procedure is repeated for all frequencies.

Values of cutting parameters T_c , D, \emptyset , n_1 and n_2 , at the roots determined from equation 3.2 is put in equation 3.2 and corresponding widths of cut are calculated.

The theoretical stability chart is shown in Fig. 16.

CHAPTER 4

DISCUSSION AND CONCLUSION

A commerison of the theoretical and the experimental stability charts is shown in Figure 17. Experimental stability chart is a straight line in the speed range of 100 to 500 rpm. Vibrations of amplitude lesser than .0125 mm are considered stable. The tool holder is stable upto a width of cut .8 mm. For widths of cut of .9 mm and 1.0 mm., vibrations are of considerable amplitude. At these widths of cut certain speeds are stable which lin in the stability regions above the envelope of threshold of stability. These stability regions are called regions of conditional stability.

Theoretical stability chart shows a rising trend for speeds lower than 200 rpm. Between 220 rpm. and 500 rpm. the theoretical stability chart is quite close to the experimental stability chart, the maximum deviation being 12.5%.

At lower cutting speeds below 200 rpm, the theoretical values are higher than the experimental values. The reason is that Kainth's (Ref.8) theoretical analysis is not applicable for the built up edge conditions which is obtained below cutting velocity of 60 m.p.m. (180 r.p.m. in the present case). However in practice carbide tools are used at cutting velocity

higher than 100 m.n.m. (300 r.p.m.), where the theoretical analysis shows fairly good agreement with the experimental results.

It is concluded that the dynamic shear angle approach is adequate to predict the threshold of stability of machine tool system.

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APPENDIX

```
THIS PROGRAM IS TO SOLVE THE EQUATIONS OF THRESHOLD C = STABILITY
$IBJOB
SIBFTC MAIN
         REAL N1, N2, N, K1
         DIMENSION FF(30), GG(30), HH(30), ROOT(500), WW(500)
         COMMON /VISHNU/THETA, K1, C, V, FI, S, N1, OMEGA, H, F, GSMALL
         COMMON /BLOCK /ROOT,M
 500
         FORMAT(1X,10F10.3)
 510
         FORMAT(1x, *FREGUETENCY*, 3F10.3)
 110
         FORMAT(8F10-1)
 210
         FORMAT (8F10.6)
         READ110, (FF(I), I=1,30)
         READ 210, (GG(I), I=1,30)
         READ_{210}, (HH(I), I=1,30)
         DG 100 I=1,30
         F = FF(I)
         GSMALL=GG(I)
         H=HH(I)
         XMIN=2.0
         XMAX=10.0
         STEP=.005
         EPS=1.*E-06
         CALLSTEEF (XMIN, XMAX, STEP, EPS)
         DO 10 J=1,M
         X = ROCT(J)
         CALL FUNC(X,F1)
         V1=V/1000.*60.
         TC=10 • * ( • 247856+1 • 5] 426*V]/10 • - • 10981*(V]/10 • ) * * 2+ • 00358*(V]/10
         •)**3-•CCCO4273*(V1/10•)**4)
         W=-SIN(FI)/TC/((GSMALL*(1.-COS(THETA))-H*SIN(THETA))*( C-N1*S*Y1
         •+2•*C/TAN(FI)))-H*OMEGA*S/V*((]•+C/TAN(FID)-K1*(]•+2•*C/TAN(FI))))
         W = (U)WW
         ROOT(J)=ROOT(J)*6n.
 10
         CONTINUE
         PRINT510, GSMALL, H, F
         PRINT500, (ROOT(J), J=1, M)
         PRINT500, (WW(J), J=1, M)
 100
         CONTINUE
         STOP
         END
$IBFTC FUNC
         SUBROUTINE FUNC(N,FF)
         REAL N1,N2,K1,N
         COMMON /VISHNU/THETA, K1, C, V, FI, S, N1, OMEGA, H, F, GSMALL
         PI=4.*ATAN(1.0)
         FD(X) = .768 + 1 .14262 \times X/100 .-.78183 \times (X/100 .) \times 2 + .2155 \times (X/100 .)
        **3-.021694*(X/100.)**4
```

```
FIA(X)=6.482+.68127*(X/10.)-.006668*(X/10.)**2
        FN1(X)=1.348*(X/100.)**(-.2715)
        FN2(X)=3.4*(X*3.281)**(-.38)
        R = 54.0
        S = .05
        V=2.*PI*R*N
        V1=V/1000.*60.
        N2=FN2(V1)
        N1=FN1(V1)
        FI=FIA(V1)*PI/180.
        D=FD(V1)
        G=S/TAN(FI)
        K1=G*N1+N2
        C=(D*COS(FI)-1•)/D/SIN(FI)
        OMEGA=2.*PI*F
        THETA=OMEGA/N*(1.-S/TAN(FI)/2./PI/R)
        FF=((H*(1.-COS(THETA))+GSMALL*SIN(THETA))*(C-N1*S*(1.+2.*C/TAN(FI))
        ))+GSMALL*OMEGA*S/V*((1.+C/TAN(FI))-K1*(1.+2.*C/TAN(FI))))
        RETURN
        END
SIBFTC STEEF
        SUBROUTINE STEEF (XMIN, XMAX, STEP, EPS)
        PROGRAM IS FOR FINDING THE ROOTS OF TRANSCIDENTAL EQATION IN THE GIVEN RANGE ITERATION FUNCTION USED REQUIRES NO DERAVATI() EVALU
C
C
         NOTATION USED ARE
C
        XMIN=MINIMUM VALUE OF INDEPANDENT VARIABLE
C
        XMAX=MAXIMUM VALUF OF INDEPANDENT VARIABLE
                                                                        ****
         STEP=STEP SIZE USED FOR SEARCHING THE VICINITY OF THE ROOT *****
        ATION STILL CONVERGENCE IS FASTER THEN NEWTON'S METHOD
                                                                        ***
         EPS=ACCURACY DESIRED FOR THE FUNCTION
         DIMENSION ROOTS (500), FUNCTN (500)
         COMMON/BLOCK/ROOTS,M
        FORMAT(10X,*NO. OF SOLUTION HAS EXCEEDED 20 *)
 100
         FORMAT(10X,14,2F12.5)
 101
         FORMAT(10X, *SORRY NO SOLUTION IN THE GIVEN RANGE *)
 102
         FORMAT(10X, *SOLUTION BY STEFFENSON'S IMPROVED REGULA FALSI METHO
 103
         D*//,10X,* NO.*5X,*ROOTS',7X,*FUNCTION*//)
         SEARCH FOR THE VICINITY 6F THE ROOT ******************
C
         X1 = XMIN
         CALL FUNC(X1,F1)
         M = 0
         IF (ABS(F1) • GT • EPS) GOTO10
C
         IS SEARCH POINT VERY CLOSE TO THE ROOT ******************
         X = X1
         F = F1
         X2=X+5.*EPS
         CALL FUNC(X2,F2)
         GOTO40
         CONTINUE
 10
         X2=X1+STEP
         CALL FUNC(X2,F2)
         IS SFARCH POINT VERY CLOSE TO THE ROOT *****************
C
         IF (ABS(F2) • GT • EPS) GOTO 20
```

```
F = F2
         X2=X+5.*EPS
         CALL FUNC(X2,F2)
         GOTO40
 20
         CONTINUE
         IF(F1*F2.LT.0.0)GOTO30
         G0T050
         CONTINUE
 30
         CALL REGULA(X1,X2,F1,F2,EPS,X,F)
 40
         CONTINUE
        M = M + 1
         IF (M.EQ.20) PRINTIO
         ROOTS(M) = X
         FUNCTN(M) = F
C
         IF(M \cdot EQ \cdot 20) PRINT101, (I, ROOTS(I), FUNCTN(I), I=1,20)
C
         IF (M.EQ.20) M=0
C
         SFARCH FOR THE NEXT ROOT STARTS *********************
 50
         CONTINUE
         X1 = X2
         F1=F2
         TEST FOR THE SEARCH DOMAIN EXOUSTED OR NOT **************
\subset
         IF(X1.LT.XMAX)GOTO10
         IF (M.EQ.O) PRINT102
         IF (M.GT.O) PRINT103
\subset
         IF(M.GT.0)PRINT101,(I,RO6TS(I),FUNCTN(I),I=1,M)
         RETURN
         END
SIBFTC REGULA
         SUBROUTINE REGULA(X1, X2, F1, F2, EPS, X3, F3)
 100
         FORMAT(10X, *NOT CONVERGING IN 30 ITERATION */)
 101
         FORMAT(10X, *ITERATION NO.*, 13)
 102
         FORMAT(10X,8F8.4)
C
         STEFFENSON'S IMPROVED REGULA FALSI ITERATION FUNCTION
C
         THIS ITERATION FUNCTION IS OF THE ORDER OF 3.23 REQUIRS NO *****
C
         DERIVATIVE EVALUATION.
                                  FUNCTION IS WITH MEMORY **********
         M = 1
         CONTINUE
 10
         X3=(X1*F2-X2*F1)/(F2-F1)
         IF(F_1*F_2 \cdot LT \cdot O \cdot O)X3 = (X1*X3-X2**2)/(X1-2 \cdot *X2+X3)
         CALL FUNC(X3,F3)
         IF (ABS(F3).LT.EPS)GOTO60
         IF(M.EQ.30)GOTO50
         CONTINUE
 20
C
         PRINT102, X1, F1, X2, F2, X3, F3
         IF(F1*F3.LT.0.0)GOTO30
         X1=X3
         F1=F3
         G0T040
 30
         CONTINUE
         F2=F3
```

```
X2=X3
CONTINUE
40
        M=M+1
        G0T010
50
        CONTINUE
C
        PRINT100
60
        CONTINUE
        X2=X3+5.0*EPS
        CALL FUNC(X2,F2)
        PRINT101,M
        RETURN
        END
SFNTRY
```

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